

# Unifying Online and Counterfactual Learning to Rank

## A Novel Counterfactual Estimator that Effectively Utilizes Online Interventions

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### Introduction

Unbiased Learning to Rank (LTR) from biased user clicks is traditionally divided into:

- **Online LTR:** Interactive algorithms that correct for bias by randomizing results.
- **Counterfactual LTR:** Algorithms that learn from historical click data, correct using a inferred model of bias.

In this paper, we bridge this traditional division by introducing a method designed for both counterfactual and online LTR:

- A counterfactual method that takes into account the effect of online interventions.

### The Intervention-Oblivious Estimator

Based on the methods of Oosterhuis and de Rijke (2020) and Vardasbi et al. (2020), we introduce a single estimator that corrects for position-bias, item-selection bias, and trust-bias. For a logging policy  $\pi$  the click probability of on an item  $d$  is an expectation over the display rank  $k$ :

$$\begin{aligned} P(C = 1 | d, \pi) &= \sum_{k=1} \pi(k | d) (\alpha_k P(R = 1 | d) + \beta_k) \\ &= \mathbb{E}_k[\alpha_k | \pi] P(R = 1 | d) + \mathbb{E}_k[\beta_k | \pi], \end{aligned}$$

where  $\alpha_k$  and  $\beta_k$  are parameters per rank and  $P(R = 1 | d)$  is the probability that a user finds  $d$  relevant.

The Intervention-Oblivious Estimator is based on the inverse:

$$P(R = 1 | d) = \frac{P(C = 1 | d, \pi) - \mathbb{E}_k[\beta_k | \pi]}{\mathbb{E}_k[\alpha_k | \pi]}.$$

This is a **counterfactual** approach: it assumes the logging policy is completely static.

### The Intervention-Aware Estimator

**Insight:** An intervention is simply a change of logging policy. Let  $\Pi$  be a set that contains the logging policy for each timestep:  $\Pi = \{\pi_1, \pi_2, \dots\}$ . The click probability can be conditioned on  $\Pi$ :

$$\begin{aligned} P(C = 1 | d, \Pi) &= \frac{1}{|\Pi|} \sum_{\pi \in \Pi} \mathbb{E}_k[\alpha_k | \pi] P(R = 1 | d) + \mathbb{E}_k[\beta_k | \pi] \\ &= \mathbb{E}_k[\alpha_k | \Pi] P(R = 1 | d) + \mathbb{E}_k[\beta_k | \Pi]. \end{aligned}$$

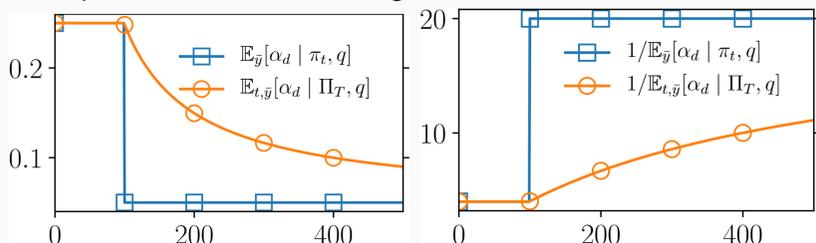
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This is a **counterfactual** and **online** approach: it takes into account online interventions for all its corrections, but it is also unbiased without any interventions.

### Visualization

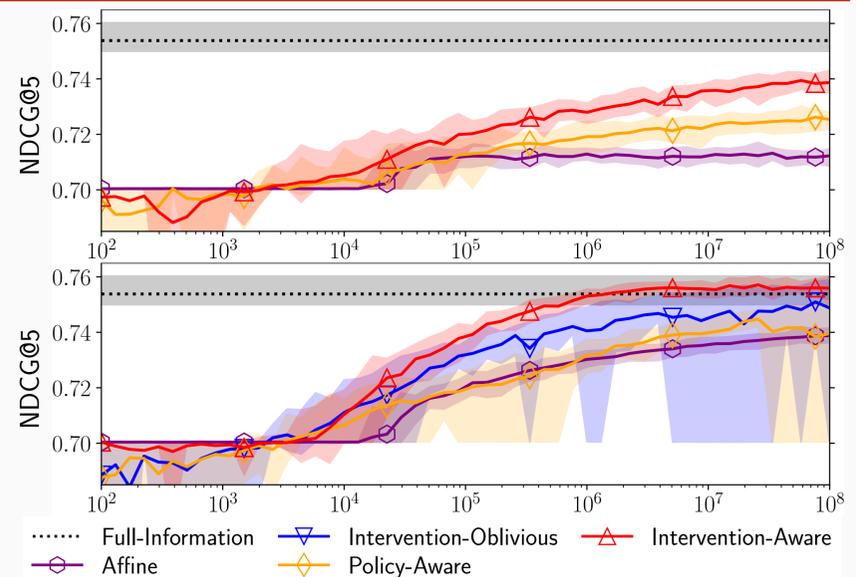
Example of the effect of a single intervention at  $t = 100$ :



### Experimental Setup

Results based on the Yahoo! Webscope dataset (Chapelle and Chang, 2011) with clicks simulated following a user model inferred by Agarwal et al. (2019) from real-world click data.

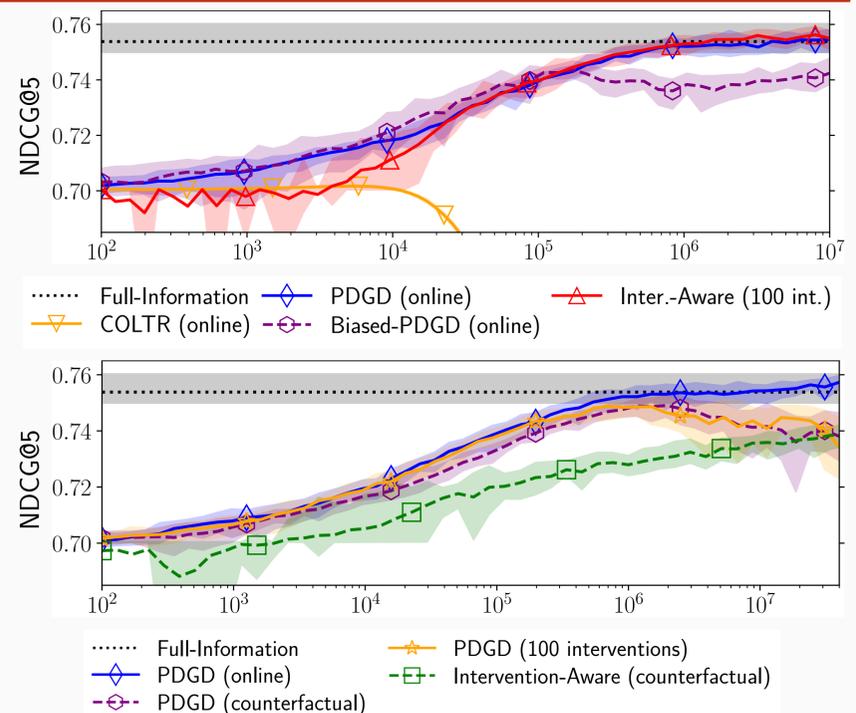
### Comparison with Counterfactual LTR



Top: Data gathered with a static policy.

Bottom: Data gathered with 50 online interventions.

### Comparison with Online LTR



### Conclusion

The intervention-aware estimator is the most reliable choice for counterfactual learning and has online performance comparable to the state-of-the-art.

**Public Code:** <https://github.com/Harrie0/2021wsdm-unifying-LTR>

### References

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