

Optimizing a Ranking System with User Interaction Logs: Counterfactual Learning to Rank



Harrie Oosterhuis

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University of Amsterdam

oosterhuis@uva.nl

Based on the SIGIR 2019 Tutorial:

Unbiased Learning to Rank: Counterfactual and Online Approaches

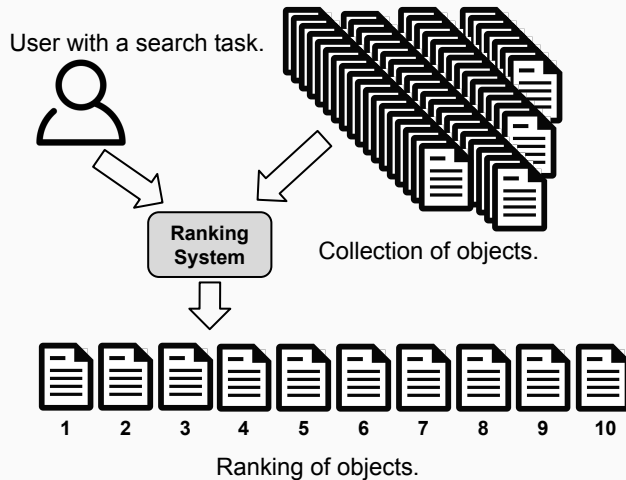
Harrie Oosterhuis, Rolf Jagerman, Maarten de Rijke

Introduction: Ranking Systems

Let's go back to the beginning:



- Ranking systems are vital for **making large document collections accessible**.
- They can present users with **a small comprehensible selection** out of **millions of unordered results**.
- Search and recommendation are **practically everywhere**.


Ranking Systems: Schematic Example





Ranking Systems: Examples


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Address: Houtlaan 4, 6525 XZ Nijmegen

Phone: 024 361 6161

Undergraduate tuition and fees: Local tuition 6,000 EUR, Domestic tuition 2,006 EUR, International tuition 17,000 EUR (2017 – 18)

Total enrollment: 19,904 (2015)


Motto: In Dei nomine feliciter (Happily in God's name, [Latin](#))

Rector: [J. H. J. M. Krieken](#)

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Information Retrieval: Implementing and Evaluating Search Engines (The MIT Press) Feb 12, 2016
by Stefan Brûcher and Charles L. A. Clarke

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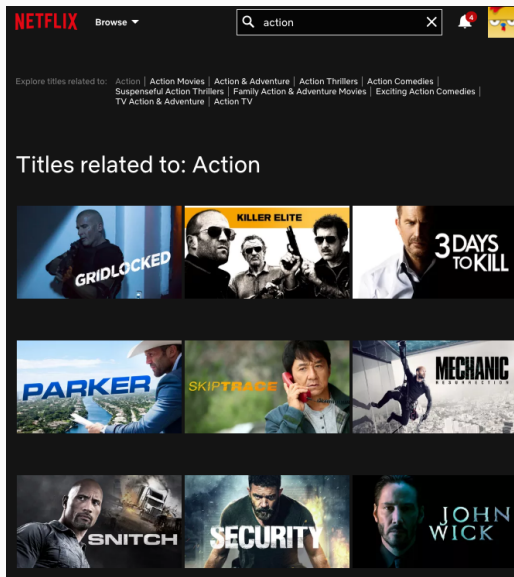
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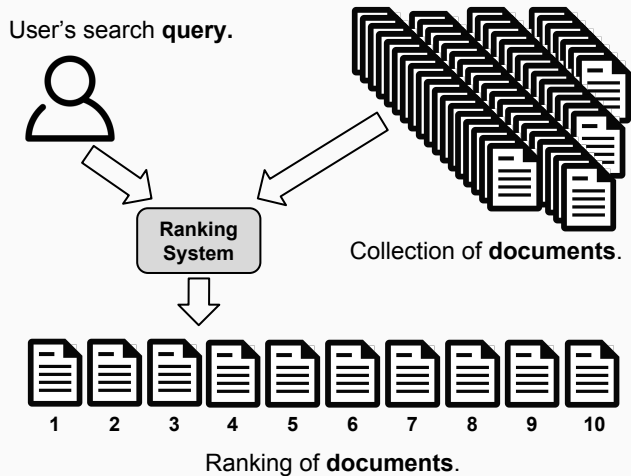
Search Engines: Information Retrieval in Practice Feb 16, 2009
by Bruce Croft and Donald Metzler

Hardcover
\$110¹⁶

Ranking Systems: Examples



Ranking Systems: Schematic Example Naming



Supervised Learning to Rank

Learning to Rank in Information Retrieval

Learning to Rank is a **core task** in informational retrieval:

- Key component for **search** and **recommendation**.

Different from **regression** where we want to scores to **match labels**,
for document d and relevance function $y(d)$ and a ranking function $f_{\theta}(d) \in \mathbb{R}$:

$$f_{\theta}(d) = y(d).$$

In **learning to rank**, we only care about the **ordering** according to f_{θ} :

$$y(d_1) > y(d_2) \rightarrow f_{\theta}(d_1) > f_{\theta}(d_2).$$

Supervised Learning to Rank

Traditionally learning to rank is **supervised** through **annotated datasets**:

- **Relevance annotations** for query-document pairs provided by **human judges**.

Over the years several limitations of annotated datasets have become apparent,

can you think of some limitations?

Limitations of the Annotated Datasets

Some of the most substantial limitations of **annotated datasets** are:

- **expensive** to make (Qin and Liu, 2013; Chapelle and Chang, 2011).
- **unethical** to create in **privacy-sensitive settings** (Wang et al., 2016).
- **impossible** for small scale problems, e.g., **personalization**.
- **stationary**, cannot capture **future changes in relevancy** (Lefortier et al., 2014).
- **not necessarily aligned with actual user preferences** (Sanderson, 2010),
i.e., annotators and users often disagree.

Limitations of the Supervised Approach

Annotated datasets are **valuable** and have an **important place in research and development**.

However, the supervised approach is:

- **Unavailable** for practitioners without a **considerable budget**.
- **Impossible** for certain ranking problems.
- Often **misaligned** with *true* user preferences.

Therefore, there is a **need** for an **alternative** learning to rank approach.

Learning from User Interactions

Learning from User Interactions: Advantages

Learning from user interactions solves the problems of annotations:

- Interactions are **virtually free** if you have users.
- User **behavior** is indicative of their **preferences**.

User interactions also bring their **own difficulties**:

- Interactions give **implicit feedback**.

Learning from User Interactions: Difficulties

User interactions bring their **own difficulties**:

- **Noise:**
 - Users click for **unexpected reasons**.
 - Often clicks occur **not because** of relevancy.
 - Often clicks do not occur **despite** of relevancy.
- **Bias:** Interactions are affected by **factors other than relevancy**:
 - **Position bias:** **Higher ranked** documents get more attention.
 - **Item selection bias:** Interactions are **limited** to the **presented** documents.
 - **Presentation bias:** Results that are **presented differently** will be **treated differently**.
 - ...

The Golden Triangle

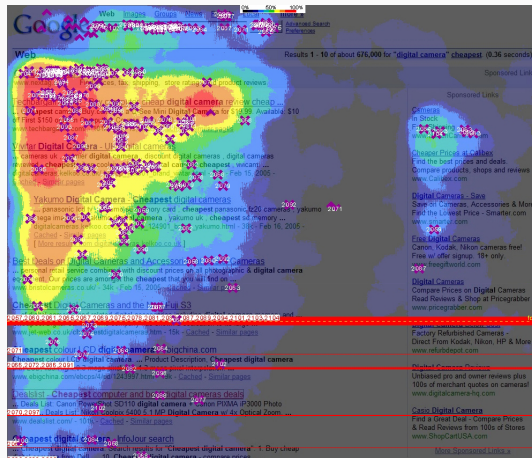


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Goal of unbiased learning to rank:

- Optimize a ranker w.r.t. **relevance preferences** of users from their interactions.
- **Avoid** being **biased by other factors** that influence interactions.

There are currently **two main approaches** to Unbiased Learning to Rank:

Online Learning to Rank

- Learning by **directly interacting with users**.
- Handle biases through **randomization of displayed results**.

Counterfactual Learning to Rank

- Learning from **historical interactions**.
- Use a **model of user behavior** to correct for biases.

We will discuss the latter.

Counterfactual Evaluation

Counterfactual Evaluation: Introduction

Evaluation is incredibly **important before deploying** a ranking system.

However, with the **limitations of annotated datasets**,
can we **evaluate** a ranker **without deploying** it or **annotated data**?

Counterfactual Evaluation:

Evaluate a new ranking function f_θ using **historical interaction data** (e.g., clicks) collected from a previously deployed ranking function f_{deploy} .

Counterfactual Evaluation: Full Information

If we **know** the **true relevance labels** ($y(d_i)$ for all i), we can compute any additive linearly decomposable IR metric as:

$$\Delta(f_\theta, D, y) = \sum_{d_i \in D} \lambda(\text{rank}(d_i \mid f_\theta, D)) \cdot y(d_i),$$

where λ is a rank weighting function, e.g.,

Average Relevant Position	$ARP : \lambda(r) = r,$
Discounted Cumulative Gain	$DCG : \lambda(r) = \frac{1}{\log_2(1 + r)},$
Precision at k	$Prec@k : \lambda(r) = \frac{\mathbf{1}[r \leq k]}{k}.$

Counterfactual Evaluation: Full Information

$$y(d_1) = 1$$

Document d_1

$$y(d_2) = 0$$

Document d_2

$$y(d_3) = 0$$

Document d_3

$$y(d_4) = 1$$

Document d_4

$$y(d_5) = 0$$

Document d_5

Counterfactual Evaluation: Partial Information

We often do not know the true relevance labels ($y(d_i)$), but can only observe implicit feedback in the form of, e.g., clicks:

- A click c_i on document d_i is a **biased and noisy indicator** that d_i is relevant
- A missing click does **not** necessarily indicate non-relevance

Counterfactual Evaluation: Clicks

$$y(d_1) = 1$$

Document d_1



$$c_1 = 1$$

$$y(d_2) = 0$$

Document d_2



$$c_2 = 0$$

$$y(d_3) = 0$$

Document d_3



$$c_3 = 1$$

$$y(d_4) = 1$$

Document d_4



$$c_4 = 0$$

$$y(d_5) = 0$$

Document d_5



$$c_5 = 0$$

Remember that there are many reasons why a click on a document may **not** occur:

- **Relevance**: the document may not be relevant.
- **Observance**: the user may not have examined the document.
- **Miscellaneous**: various random reasons why a user may not click.

Some of these reasons are considered to be:

- **Noise**: averaging over many clicks will remove their effect.
- **Bias**: averaging will **not** remove their effect.

Counterfactual Evaluation: Examination User Model

If we **only** consider **examination** and **relevance**, a user click can be modelled by:

- The probability of document d_i **being examined** ($o_i = 1$) in a ranking R :

$$P(o_i = 1 \mid R, d_i)$$

- The probability of a **click** $c_i = 1$ on d_i given its **relevance** $y(d_i)$ and whether it was **examined** o_i :

$$P(c_i = 1 \mid o_i, y(d_i))$$

- **Clicks only occur on examined documents**, thus the probability of a click in ranking R is:

$$P(c_i = 1 \wedge o_i = 1 \mid y(d_i), R) = P(c_i = 1 \mid o_i = 1, y(d_i)) \cdot P(o_i = 1 \mid R, d_i)$$

Counterfactual Evaluation: Naive Estimator

A **naive way** to estimate is to assume clicks are a unbiased relevance signal:

$$\Delta_{NAIVE}(f_{\theta}, D, c) = \sum_{d_i \in D} \lambda(\text{rank}(d_i \mid f_{\theta}, D)) \cdot c_i.$$

Even if **no click noise** is present: $P(c_i = 1 \mid o_i = 1, y(d_i)) = y(d_i)$, this estimator is **biased** by the examination probabilities:

$$\begin{aligned} \mathbb{E}_o[\Delta_{NAIVE}(f_{\theta}, D, c)] &= \mathbb{E}_o \left[\sum_{d_i \in D} c_i \cdot \lambda(\text{rank}(d_i \mid f_{\theta}, D)) \right] \\ &= \mathbb{E}_o \left[\sum_{d_i \in D} o_i \cdot y(d_i) \cdot \lambda(\text{rank}(d_i \mid f_{\theta}, D)) \right] \\ &= \sum_{d_i \in D} P(o_i = 1 \mid R, d_i) \cdot \lambda(\text{rank}(d_i \mid f_{\theta}, D)) \cdot y(d_i). \end{aligned}$$

Counterfactual Evaluation: Naive Estimator Bias

The biased estimator **weights documents** according to their **examination probabilities** in the ranking R displayed during **logging**:

$$\mathbb{E}_o[\Delta_{NAIVE}(f_\theta, D, c)] = \sum_{d_i \in D} P(o_i = 1 \mid R, d_i) \cdot \lambda(\text{rank}(d_i \mid f_\theta, D)) \cdot y(d_i).$$

In rankings, **documents at higher ranks** are more likely to be examined: **position bias**.

What effect does this have on the evaluation?

Counterfactual Evaluation: Naive Estimator Bias

The biased estimator **weights documents** according to their **examination probabilities** in the ranking R displayed during **logging**:

$$\mathbb{E}_o[\Delta_{NAIVE}(f_\theta, D, c)] = \sum_{d_i \in D} P(o_i = 1 \mid R, d_i) \cdot \lambda(\text{rank}(d_i \mid f_\theta, D)) \cdot y(d_i).$$

In rankings, **documents at higher ranks** are more likely to be examined: **position bias**.

Position bias causes **logging-policy-confirming** behavior:

- Documents displayed at **higher ranks during logging** are incorrectly considered as **more relevant**.

Inverse Propensity Scoring

Counterfactual Evaluation: Inverse Propensity Scoring

Counterfactual evaluation accounts for bias using **Inverse Propensity Scoring (IPS)**:

$$\Delta_{IPS}(f_{\theta}, D, c) = \sum_{d_i \in D} \frac{\lambda(\text{rank}(d_i \mid f_{\theta}, D))}{P(o_i = 1 \mid R, d_i)} \cdot c_i,$$

- $\lambda(\text{rank}(d_i \mid f_{\theta}, D))$: (weighted) rank of document d_i by ranker f_{θ} ,
- c_i : observed click on the document in the log,
- $P(o_i = 1 \mid R, d_i)$: examination probability of d_i in ranking R displayed during logging.

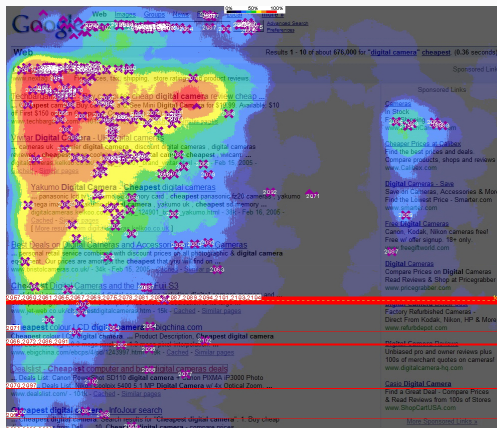
This is an **unbiased estimate** of any additive linearly decomposable IR metric.

Counterfactual Evaluation: Proof of Unbiasedness

If no click noise is present, this provides an **unbiased estimate**:

$$\begin{aligned}\mathbb{E}_o[\Delta_{IPS}(f_\theta, D, c)] &= \mathbb{E}_o \left[\sum_{d_i \in D} \frac{\lambda(\text{rank}(d_i \mid f_\theta, D))}{P(o_i = 1 \mid R, d_i)} \cdot c_i \right] \\&= \mathbb{E}_o \left[\sum_{d_i \in D} \frac{o_i \cdot \lambda(\text{rank}(d_i \mid f_\theta, D)) \cdot y(d_i)}{P(o_i = 1 \mid R, d_i)} \right] \\&= \sum_{d_i \in D} \frac{P(o_i = 1 \mid R, d_i) \cdot \lambda(\text{rank}(d_i \mid f_\theta, D)) \cdot y(d_i)}{P(o_i = 1 \mid R, d_i)} \\&= \sum_{d_i \in D} \lambda(\text{rank}(d_i \mid f_\theta, D)) \cdot y(d_i) \\&= \Delta(f_\theta, D, y).\end{aligned}$$

Remember the Golden Triangle?



The IPS estimator weights clicks inversely proportional to the examination probabilities.

Counterfactual Evaluation: Robustness of Noise

So far we have **assumed no click noise**: $P(c_i = 1 \mid o_i = 1, y(d_i)) = y(d_i)$.

However, the IPS approach still works without this assumption, as long as:

$$y(d_i) > y(d_j) \Leftrightarrow P(c_i = 1 \mid o_i, y(d_i)) > P(c_j = 1 \mid o_j, y(d_j)).$$

Since we can prove **relative differences** are inferred unbiasedly:

$$\mathbb{E}_{o,c}[\Delta_{IPS}(f_\theta, D, c)] > \mathbb{E}_{o,c}[\Delta_{IPS}(f_{\theta'}, D, c)] \Leftrightarrow \Delta(f_\theta, D) > \Delta(f_{\theta'}, D).$$

Propensity-weighted Learning to Rank

Propensity-weighted Learning to Rank (LTR)

The inverse-propensity-scored estimator can unbiasedly estimate performance:

$$\Delta_{IPS}(f_{\theta}, D, c) = \sum_{d_i \in D} \frac{\lambda(\text{rank}(d_i \mid f_{\theta}, D))}{P(o_i = 1 \mid R, d_i)} \cdot c_i.$$

How do we **optimize** for this **unbiased performance estimate**?

- It is **not differentiable**.
- **Common problem for all ranking metrics**.

Upper Bound on Rank

Rank-SVM (Joachims, 2002) optimizes the following **differentiable upper bound**:

$$\begin{aligned} \text{rank}(d \mid f_\theta, D) &= \sum_{d' \in R} \mathbb{1}[f_\theta(d) \leq f_\theta(d')] \\ &\leq \sum_{d' \in R} \max(1 - (f_\theta(d) - f_\theta(d')), 0) = \overline{\text{rank}}(d \mid f_\theta, D). \end{aligned}$$

Alternative choices are possible, i.e., a **sigmoid-like bound** (with parameter σ):

$$\text{rank}(d \mid f_\theta, D) \leq \sum_{d' \in R} \log_2(1 + \exp^{-\sigma(f_\theta(d) - f_\theta(d'))}).$$

Commonly used for pairwise learning, LambdaMart (Burges, 2010), and Lambdaloss (Wang et al., 2018b).

Propensity-weighted LTR: Average Relevance Position

Then for the Average Relevance Position metric:

$$\Delta_{ARP}(f_{\theta}, D, y) = \sum_{d_i \in D} \text{rank}(d_i \mid f_{\theta}, D) \cdot y(d_i).$$

This gives us an **unbiased estimator** and **upper bound**:

$$\begin{aligned} \Delta_{ARP-IPS}(f_{\theta}, D, c) &= \sum_{d_i \in D} \frac{\text{rank}(d_i \mid f_{\theta}, D)}{P(o_i = 1 \mid R, d_i)} \cdot c_i \\ &\leq \sum_{d_i \in D} \frac{\overline{\text{rank}}(d_i \mid f_{\theta}, D)}{P(o_i = 1 \mid R, d_i)} \cdot c_i, \end{aligned}$$

This upper bound is **differentiable** and **optimizable** by stochastic gradient descent or Quadratic Programming, i.e., Rank-SVM (Joachims, 2006).

Propensity-weighted LTR: Additive Metrics

A similar approach can be applied to **additive metrics** (Agarwal et al., 2019).

If λ is a **monotonically decreasing** function:

$$x \leq y \Rightarrow \lambda(x) \geq \lambda(y),$$

then:

$$\text{rank}(d \mid \cdot) \leq \overline{\text{rank}}(d \mid \cdot) \Rightarrow \lambda(\text{rank}(d \mid \cdot)) \geq \lambda(\overline{\text{rank}}(d \mid \cdot)).$$

This provides a **lower bound**, for instance for Discounted Cumulative Gain (DCG):

$$\frac{1}{\log_2(1 + \text{rank}(d \mid \cdot))} \geq \frac{1}{\log_2(1 + \overline{\text{rank}}(d \mid \cdot))}.$$

Propensity-weighted LTR: Discounted Cumulative Gain

Then for the Discounted Cumulative Gain metric:

$$\Delta_{DCG}(f_{\theta}, D, y) = \sum_{d_i \in D} \log_2(1 + \text{rank}(d_i \mid f_{\theta}, D))^{-1} \cdot y(d_i).$$

This gives us an **unbiased estimator** and **lower bound**:

$$\begin{aligned} \Delta_{DCG-IPS}(f_{\theta}, D, c) &= \sum_{d_i \in D} \frac{\log_2(1 + \text{rank}(d_i \mid f_{\theta}, D))^{-1}}{P(o_i = 1 \mid R, d_i)} \cdot c_i \\ &\geq \sum_{d_i \in D} \frac{\log_2(1 + \overline{\text{rank}}(d_i \mid f_{\theta}, D))^{-1}}{P(o_i = 1 \mid R, d_i)} \cdot c_i. \end{aligned}$$

This lower bound is **differentiable** and **optimizable** by stochastic gradient descent or the Convex-Concave Procedure (Agarwal et al., 2019).

Propensity-weighted LTR: Walkthrough

Overview of the approach:

- Obtain a **model of position bias**.
- Acquire a **large click-log**.
- Then for every click in the log:
 - Compute the **propensity of the click**:

$$P(o_i = 1 \mid R, d_i).$$

- Calculate the **gradient** of the **bound** on the **unbiased estimator**:

$$\nabla_{\theta} \left[\frac{\lambda(\overline{\text{rank}}(d_i \mid f_{\theta}, D))}{P(o_i = 1 \mid R, d_i)} \right].$$

- **Update the model** f_{θ} by adding/subtracting the gradient.

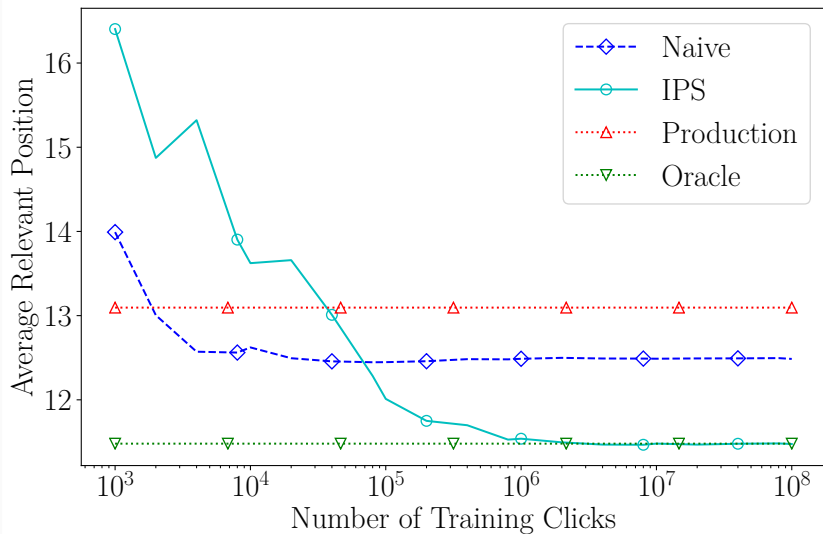
Propensity-weighted LTR: Semi-synthetic Experiments

Unbiased LTR methods are commonly **evaluated** through **semi-synthetic experiments** (Joachims, 2002; Agarwal et al., 2019; Jagerman et al., 2019).

The experimental setup:

- Traditional LTR dataset, e.g., Yahoo! Webscope (Chapelle and Chang, 2011).
- Simulate queries by uniform sampling from the dataset.
- Create a ranking according to a baseline ranker.
- Simulate clicks by modelling:
 - **Click Noise**, e.g., 10% chance of clicking on a non-relevant document.
 - **Position Bias**, e.g., $P(o_i = 1 \mid R, d_i) = \frac{1}{\text{rank}(d \mid R)}$.
- Hyper-parameter tuning by unbiased evaluation methods.

Propensity-weighted LTR: Results



So far we have seen how to:

- Perform **Counterfactual Evaluation** with **unbiased estimators**.
- Perform **Counterfactual LTR** by optimizing **unbiased estimators**.

What essential part are we still missing?

Estimating Position Bias

Recall that position bias is a form of bias where higher positioned results are more likely to be observed and therefore clicked.

Assumption: The **observation probability** only depends on the rank of a document:

$$P(o_i = 1 \mid i).$$

The objective is now to **estimate**, for each rank i , the propensity $P(o_i = 1 \mid i)$.

Estimating Position Bias

So far we have seen how to:

- Perform **Counterfactual Evaluation** with **unbiased estimators**.
- Perform **Counterfactual LTR** by optimizing **unbiased estimators**.

At the core of these methods is the propensity score: $P(o_i = 1 \mid R, d_i)$, which helps remove bias from user interactions.

In this section, we will show how this **propensity score** can be **estimated** for a specific kind of bias: **position bias**.

Estimating Position Bias

Recall that position bias is a form of bias where higher positioned results are more likely to be observed and therefore clicked.

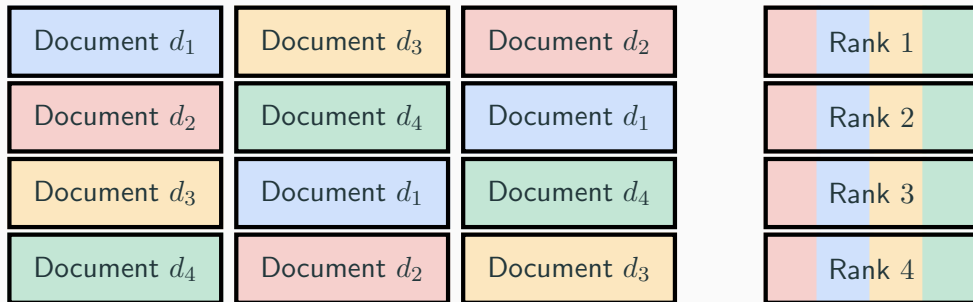
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$$P(o_i = 1 \mid i).$$

The objective is now to **estimate**, for each rank i , the propensity $P(o_i = 1 \mid i)$.

Estimating Position Bias

RandTop- n Algorithm:



RandTop- n Algorithm:

- ① Repeat:
 - Randomly shuffle the top n items
 - Record clicks
- ② Aggregate clicks per rank
- ③ Normalize to obtain propensities $p_i \propto P(o_i \mid i)$

Note: we only need propensities proportional to the true observation probability for learning.

Uniformly **randomizing** the top n results may negatively impacts users during data logging.

There are various methods that minimize the impact to the user:

- RandPair: Choose a pivot rank k and only swap a random other document with the document at this pivot rank (Joachims et al., 2017).
- Interventional Sets: Exploit inherent “randomness” in data coming from multiple rankers (e.g., A/B tests in production logs) (Agarwal et al., 2017).

What is the downside of estimating propensities through randomization?

Jointly Learning and Estimating

In the previous sections we have seen:

- Counterfactual ranker evaluation with unbiased estimators.
- Counterfactual LTR by optimizing unbiased estimators.
- Estimating propensity scores through randomization.

Instead of treating **propensity estimation** and **unbiased learning to rank** as two separate tasks, recent work has explored **jointly learning rankings and estimating propensities**.

Recall that the probability of a click can be decomposed as:

$$\underbrace{P(c_i = 1 \wedge o_i = 1 \mid y(d_i), R)}_{\text{click probability}} = \underbrace{P(c_i = 1 \mid o_i = 1, y(d_i))}_{\text{relevance probability}} \cdot \underbrace{P(o_i \mid R, d_i)}_{\text{observation probability}} .$$

In the previous sections we have seen that, if the **observation probability** is known, we can find an unbiased estimate of relevance via IPS.

Jointly Learning and Estimating

It is possible to **jointly learn and estimate** by iterating two steps:

- 1 Learn an optimal ranker given a correct propensity model:

$$\underbrace{P(c_i = 1 \mid o_i = 1, y(d_i))}_{\text{relevance probability}} = \frac{P(c_i = 1 \wedge o_i = 1 \mid y(d_i), R)}{P(o_i \mid R, d_i)}.$$

- 2 Learn an optimal propensity model given a correct ranker:

$$\underbrace{P(o_i \mid R, d_i)}_{\text{observation probability}} = \frac{P(c_i = 1 \wedge o_i = 1 \mid y(d_i), R)}{P(c_i = 1 \mid o_i = 1, y(d_i))}.$$

- Given an accurate **model of relevance**, it is possible to find an accurate **propensity model**, and vice versa.
- This approach requires **no randomization**.
- Recent work has solved this via either an **Expectation-Maximization approach** (Wang et al. (2018a)) or a **Dual Learning Objective** (Ai et al. (2018)).

Conclusion

In this lecture we discussed:

- **User-interactions** on rankings are **very biased**.
- **Counterfactual Learning to Rank:**
 - Unbiased learning from historical interaction logs.
 - Correct for position bias with inverse propensity scoring.
 - Requires an explicit user model.
- Estimating **users' examination probabilities:**
 - Through randomization or joint learning.

Future Directions

- **Unbiased Learning to Rank for:**
 - Recommender systems (Schnabel et al., 2016).
 - Personalized rankings in search or recommendation.
- **Correcting for more biases:**
 - Presentation bias, a well known but unaddressed bias.
 - Social biases (fair/ethical A.I.) especially when ranking people.
- **Learning from other signals:**
 - Likes, dwell time, conversion, purchases, watch-time, etc.

This is an extremely active area of research!

Thank you for participating!

Notation

Definition	Notation	Example
Query	q	—
Candidate documents	D	—
Document	$d \in D$	—
Ranking	R	(R_1, R_2, \dots, R_n)
Document at rank i	R_i	$R_i = d$
Relevance	$y : D \rightarrow \mathbb{N}$	$y(d) = 2$
Ranker model with weights θ	$f_\theta : D \rightarrow \mathbb{R}$	$f_\theta(d) = 0.75$
Click	$c_i \in \{0, 1\}$	—
Observation	$o_i \in \{0, 1\}$	—
Rank of d when f_θ ranks D	$\text{rank}(d \mid f_\theta, D)$	$\text{rank}(d \mid f_\theta, D) = 4$

Differentiable upper bound on $rank(d, f_{\theta}, D)$	$\overline{rank}(d, f_{\theta}, D)$	–
Average Relevant Position metric	ARP	–
Discounted Cumulative Gain metric	DCG	–
Precision at k metric	$Prec@k$	–
A performance measure or estimator	Δ	–

- Tensorflow Learning to Rank, allows for inverse propensity scoring:
<https://github.com/tensorflow/ranking>
- Inverse Propensity Score Rank-SVM:
https://www.cs.cornell.edu/people/tj/svm_light/svm_proprank.html
- Data and code for comparing counterfactual and online learning to rank
<http://github.com/rjagerman/sigir2019-user-interactions>
- An older online learning to rank framework: Lerot
<https://bitbucket.org/ilps/lerot/>

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