

Policy-Aware Unbiased Learning to Rank for Top-k Rankings

Harrie Oosterhuis¹, Maarten de Rijke^{2,3}

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Radboud University¹, University of Amsterdam², Ahold Delhaize³

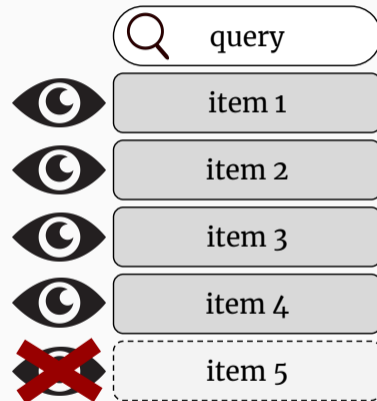
harrie.oosterhuis@ru.nl, derijke@uva.nl

<https://twitter.com/HarrieOos>

Introduction: Top-k Ranking

Top-k ranking: very prevalent in **search** and **recommendation**.

Goal: optimize a ranking model for top-k ranking.



Background:

Counterfactual Learning to Rank



Learn from **historically logged user clicks** (Joachims et al., 2017; Wang et al., 2016).

Problem:

- Clicks are **biased indicators** of preference (Craswell et al., 2008).

Existing solution:

- **Weight clicks** to correct for position bias.



For an item d , displayed ranking \bar{R} , and query q ,

decompose the click probability according to examination hypothesis:

$$P(C = 1 \mid \bar{R}, q, d) = \overbrace{P(E = 1 \mid \bar{R}, d)}^{\text{examination}} \overbrace{P(C = 1 \mid E = 1, q, d)}^{\text{relevance}}. \quad (1)$$



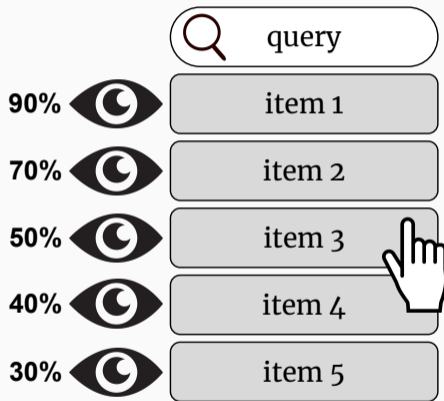
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Existing work corrects for position bias by **Inverse Propensity Scoring** (Joachims et al., 2017; Wang et al., 2016). Given N displayed rankings for query q :

$$\text{relevance}(q, d) \approx \frac{1}{N} \sum_{i=1}^N \frac{c_i}{P(E = 1 \mid \bar{R}_i, d)}. \quad (2)$$



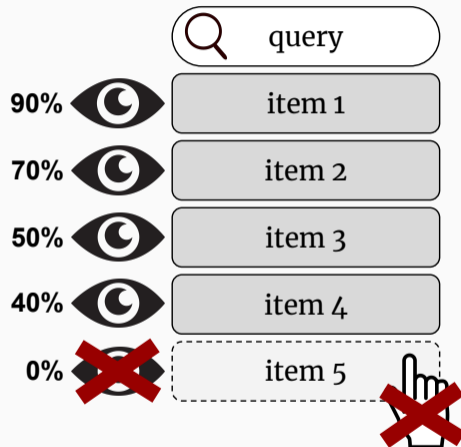
Item-Selection Bias

Items that are **not displayed cannot be examined**:

$$\text{rank}(d \mid \bar{R}) > k \rightarrow P(E = 1 \mid \bar{R}_i, d) = 0. \quad (3)$$

Existing approach does **not work in top-k rankings**:

- No clicks to weight!



The Novel Policy-Aware Estimator



If displayed rankings are sampled from a **stochastic policy** π ,
the click probability can be **conditioned** on the **policy**:

$$P(C = 1 \mid \pi, q, d) = \sum_{\bar{R}} \overbrace{\pi(\bar{R} \mid q)}^{\text{policy}} \overbrace{P(E = 1 \mid \bar{R}, d)}^{\text{examination}} \overbrace{P(C = 1 \mid E = 1, q, d)}^{\text{relevance}}. \quad (4)$$



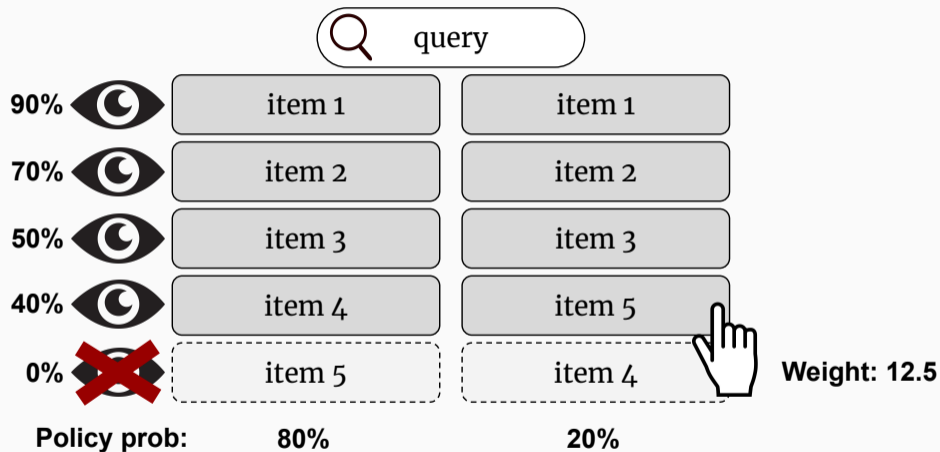
If displayed rankings are sampled from a **stochastic policy** π , the click probability can be **conditioned** on the **policy**:

$$P(C = 1 \mid \pi, q, d) = \sum_{\bar{R}} \overbrace{\pi(\bar{R} \mid q)}^{\text{policy}} \overbrace{P(E = 1 \mid \bar{R}, d)}^{\text{examination}} \overbrace{P(C = 1 \mid E = 1, q, d)}^{\text{relevance}}. \quad (4)$$

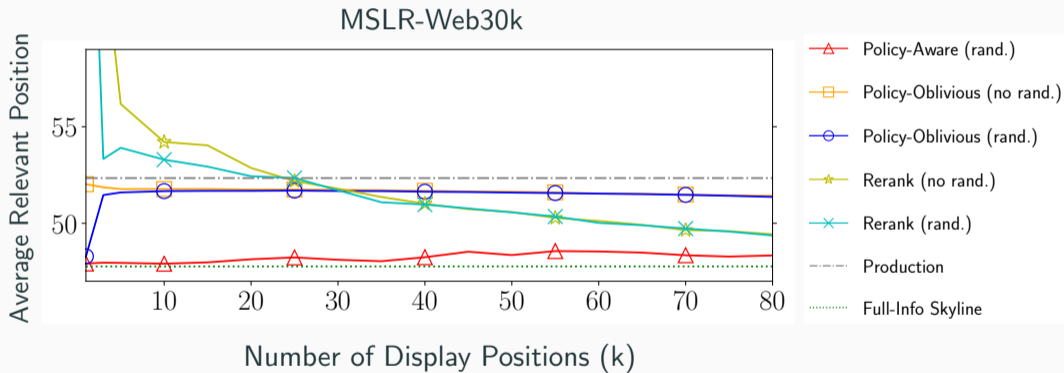
Our **Policy-Aware Estimator** weights conditioned on the policy:

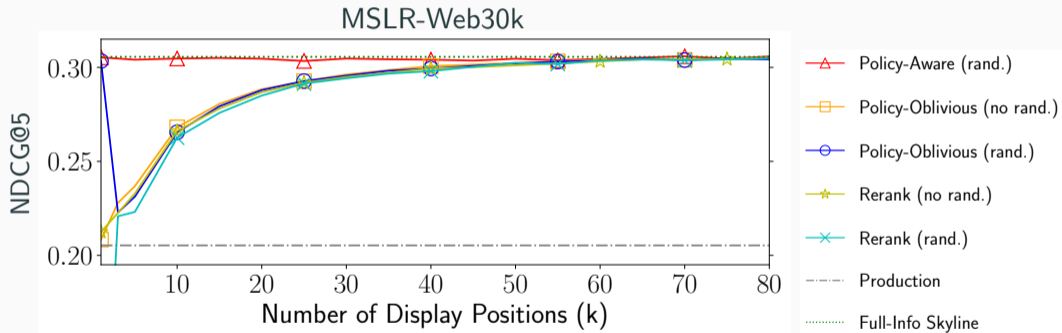
$$\text{relevance}(q, d) \approx \frac{1}{N} \sum_{i=1}^N \frac{c_i}{P(E = 1 \mid \pi, d)} = \frac{1}{N} \sum_{i=1}^N \frac{c_i}{\sum_{\bar{R}} \pi(\bar{R} \mid q) P(E = 1 \mid \bar{R}, d)}. \quad (5)$$

Unbiased if every item has a **non-zero chance** of being displayed in the top-k.



Experimental Results





Conclusion



Main takeaways:

- Existing Counterfactual LTR cannot correct item-selection bias.
- Novel Policy-Aware estimator can under mild randomization.
- Adapted LambdaLoss works for counterfactual LTR
(Not discussed in presentation).



- N. Craswell, O. Zoeter, M. Taylor, and B. Ramsey. An experimental comparison of click position-bias models. In *Proceedings of the 2008 International Conference on Web Search and Data Mining*, pages 87–94. ACM, 2008.
- T. Joachims, A. Swaminathan, and T. Schnabel. Unbiased learning-to-rank with biased feedback. In *Proceedings of the Tenth ACM International Conference on Web Search and Data Mining*, pages 781–789. ACM, 2017.
- X. Wang, M. Bendersky, D. Metzler, and M. Najork. Learning to rank with selection bias in personal search. In *Proceedings of the 39th International ACM SIGIR conference on Research and Development in Information Retrieval*, pages 115–124. ACM, 2016.



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MSLR-Web30k - top-5 setting

